\mathcal{H} iggs \mathcal{P} hysics

M. Margarete Mühlleitner (Karlsruhe Institute of Technology, KIT)

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• Standard Model Higgs Sector

- Introduction
- Verification of the Higgs mechanism
 - Higgs discovery production and decay
 - Determination of Higgs boson couplings
 - Determination of Spin and CP quantum numbers
 - Determination of the Higgs self-couplings

• Beyond Standard Model Higgs Sectors (maybe)

- Minimal Supersymmetric Extension of the SM (MSSM)
 - LHC results and MSSM Higgs sector
- Next-Minimal Supersymmetric Extension of the SM (NMSSM)
 - LHC results and NMSSM Higgs sector

• Local gauge symmetry group $SU(3) \times SU(2)_L \times U(1)_Y$



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Construction of the SM Lagrangian

- ◊ Particle content
- ◊ Poincaré invariance
- \diamond Local gauge invariance under $SU(3) \times SU(2) \times U(1)$
- ◊ Renormalizability
- ◇ Mechanism of electroweak symmetry breaking

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Construction of the SM Lagrangian

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$$\begin{aligned} \mathcal{L} &= -\frac{1}{4} F^{a}_{\mu\nu} F^{a\mu\nu} + i \bar{\psi} D \psi & \text{gauge sector} \\ &+ \psi_i \lambda_{ij} \psi_j H & \text{flavour sector} \\ &|DH|^2 - V(H) & \text{EWSB sector} \\ &+ N_i M_{ij} N_j & \nu \text{- mass sector} & \text{not taken into account here} \end{aligned}$$

Gauge symmetry forbids mass terms for gauge bosons and fermions!

Free parameters of the Standard Model: at least 26!

- 3 gauge couplings
- 1 CP-violating vacuum angle
- 6 quark masses
- 3 charged lepton masses
- 3 weak mixing angles
- 1 CP-violating CKM phase
- 1 W-mass
- 1 Higgs mass
- and the neutrino sector
 - 3 neutrino masses
 - 3 neutrino mixing angles
 - 3 CP-violating phases

\mathcal{T} he \mathcal{H} iggs \mathcal{M} echanism

Brout-Englert-Higgs-Hagen-Guralnik-Kibble-Mechanism 1964



\mathcal{T} he \mathcal{H} iggs \mathcal{M} echanism

- Why do we need the Higgs Mechanism?
- * Standard Model (SM) based on symmetries: $SU(3)_C imes SU(2)_L imes U(1)_Y$
- * Symmetries associated with existence of gauge bosons massive gauge bosons (W^{\pm} , Z) and massless gauge bosons (photon, gluons)
- * Mass terms of massive gauge bosons violate the SM symmetries

• Solution:

- * Mechanism which introduces particle masses without violating the SM gauge symmetries
- Realisation:
- * Higgs Mechanism





Electroweak Symmetry Breaking

- How does it work? Mass generation via spontaneous symmetry breaking (SSB)
- Add Higgs field with Higgs potential to SM Lagrangian
- Higgs potential respects SM symmetries non-vanishing vacuum expectation value (VEV) in the ground state
- \circ Choose one of the infinite degenerate ground states as the physical ground state
- $\circ \; SU(2)_L \times U(1)_Y$ hidden, broken down to $U(1)_{em}$
- \circ Particles acquire mass through interaction with scalar field in the ground state
- \circ Non-vanishing VEV $v=246~{\rm GeV}$
 - \leftarrow typical minimax form of the Higgs potential



$\mathcal From \ WW \ \mathcal Scattering to the \ \mathcal Higgs \ \mathcal Boson$

• Fermi theory: describes weak interaction with an effective Lagrangian

E.g.
$$\mu$$
 decay: $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$

$$\mathcal{L} = \frac{G_F}{\sqrt{2}} [\bar{\nu}_{\mu} \gamma_{\lambda} (1 - \gamma_5) \mu] [\bar{e} \gamma^{\lambda} (1 - \gamma_5) \nu_e]$$

- $G_F \approx 1.17 \times 10^{-5} \text{ GeV}^{-2}$ (Fermi coupling)
- Fermi theory at high energies: $\mathcal{M}[\nu_{\mu}e^{-} \rightarrow \mu^{-}\nu_{e}] \sim \frac{G_{F}}{2\sqrt{2}\pi}s \Rightarrow$ violates unitarity



$$\mathcal{M}[\nu_{\mu}e^{-} \to \mu^{-}\nu_{e}] \to \frac{G_{F}s}{2\sqrt{2}\pi} \frac{M_{W}^{2}}{M_{W}^{2}-s} \quad \text{(with } M_{W} \approx 100 \text{ GeV)}$$

• Scattering of longitudinally polarized W bosons





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• Scattering of longitudinally polarized W bosons



Higgs particle guarantees unitarity of the W scattering (if its mass ≤ 1 TeV, $g_{XXH} \sim$ particle mass M_X ; also unitarity in $WW \rightarrow hh$, $WW \rightarrow ff$)

A theory with massive gauge bosons and fermions, which is weakly coupled up to very high energies, requires, because of the demand for unitarity, the existence of a Higgs particle. The Higgs particle is a scalar 0⁺ particle, which couples to other particles with a coupling proportional to the mass of the particle. Goal: generate W and Z boson masses without violating gauge invariance. Toy model:

 \vartriangleright Local U(1) gauge theory with single spin-1 gauge field A_{μ}

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$
 where $F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$

 \rightarrow mass term $\sim m^2 A^\mu A_\mu$ not gauge invariant \rightsquigarrow massless gauge boson A

 \triangleright Possible solution: add complex scalar field ϕ $(D_{\mu} = \partial_{\mu} + ieA_{\mu})$

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + |D_{\mu}\phi|^2 - V(\phi) \quad \text{where} \quad V(\phi) = \mu^2 |\phi|^2 + \lambda |\phi|$$

if $\mu^2 > 0$: unique minimum at $\phi = 0 \rightarrow \text{QED}$ with $M_A = 0$ and $M_\phi = \mu$

 \vartriangleright Reverse sign of μ^2 so that $V(\phi) = -(-\mu^2) |\phi|^2 + \lambda |\phi|^4$

 \rightarrow minimum of the potential at $\sqrt{-\frac{\mu^2}{2\lambda}}\equiv v$

 \triangleright Expand ϕ around the vacuum expectation value $v: \phi = v + \frac{1}{\sqrt{2}}(H + i\chi) \Rightarrow$

 $\mu^2 > 0$



 $\mu^2 < 0$

\mathcal{C} alculation

Potential:

$$V(\phi) = -(-\mu^2)|\phi|^2 + \lambda|\phi|^4 \quad \text{and} \quad \phi = v + \frac{1}{\sqrt{2}}(H + i\chi) \quad , \quad -\mu^2 = 2\lambda v^2 \quad \Rightarrow \tag{1}$$

$$V = -(-\mu^{2})\left(v^{2} + \frac{H^{2}}{2} + \sqrt{2}Hv + \frac{\chi^{2}}{2}\right)$$

+ $\lambda\left(v^{4} + \frac{H^{4}}{4} + v^{2}H^{2} + 2H^{2}v^{2} + 2\sqrt{2}Hv^{3} + \sqrt{2}H^{3}v + \frac{\chi^{4}}{4} + \frac{2v^{2}\chi^{2}}{2} + \frac{H^{2}\chi^{2}}{2} + \frac{2\sqrt{2}Hv\chi^{2}}{2}\right)$
= $\mu^{2}v^{2} + \left(-\frac{(-\mu^{2})}{2} + 3\lambda v^{2}\right)H^{2} + \sqrt{2}\lambda vH(H^{2} + \chi^{2}) + \frac{\lambda}{4}(H^{4} + 2H^{2}\chi^{2} + \chi^{4})$
+ $\sqrt{2}\mu^{2}Hv + 2\sqrt{2}\lambda Hv^{3} + \frac{\mu^{2}\chi^{2}}{2} + \frac{2\lambda v^{2}\chi^{2}}{2} + \lambda v^{4}$
= $-\mu^{2}H^{2} + \sqrt{2}\lambda vH(H^{2} + \chi^{2}) + \frac{\lambda}{4}(H^{2} + \chi^{2})^{2} + \text{const.}$ (2)

$$\begin{aligned} \mathcal{L} &= -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + (\partial_{\mu} + ieA_{\mu})\left(v + \frac{1}{\sqrt{2}}(H + i\chi)\right)(\partial^{\mu} - ieA^{\mu})\left(v + \frac{1}{\sqrt{2}}(H - i\chi)\right) - V(\phi) \\ &= -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}\partial_{\mu}(H + i\chi)\partial^{\mu}(H - i\chi) + \frac{1}{2}(ieA_{\mu})(H + i\chi)\partial^{\mu}(H - i\chi) \\ &+ \frac{1}{2}(H - i\chi)\partial_{\mu}(H + i\chi)(-ieA^{\mu}) + v^{2}e^{2}A_{\mu}A^{\mu} + \frac{ieA_{\mu}}{\sqrt{2}}(H + i\chi)\frac{(-ieA^{\mu})}{\sqrt{2}}(H - i\chi) \\ &+ (-ieA^{\mu})(ieA_{\mu})v\frac{1}{\sqrt{2}}(H - i\chi) + (ieA^{\mu})(-ieA_{\mu})v\frac{1}{\sqrt{2}}(H + i\chi) + \sqrt{2}evA_{\mu}\partial^{\mu}\chi - V(\phi) \\ &= -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}(\partial_{\mu}H)(\partial^{\mu}H) + \frac{1}{2}(\partial_{\mu}\chi)(\partial^{\mu}\chi) + \frac{1}{2}(2v^{2}e^{2})A_{\mu}A^{\mu} \\ &+ \frac{i^{2}}{2}eA_{\mu}\chi(\partial^{\mu}H) + \frac{(-i)i}{2}eA_{\mu}H(\partial^{\mu}\chi) + \frac{(-i)^{2}}{2}eA^{\mu}(\partial_{\mu}H)\chi + \frac{(-i)i}{2}eA^{\mu}(\partial_{\mu}\chi)H \\ &+ \frac{e^{2}}{2}A_{\mu}A^{\mu}(H^{2} + \chi^{2} + 2\sqrt{2}vH) + \sqrt{2}evA_{\mu}\partial^{\mu}\chi - V(\phi) \end{aligned}$$

Electroweak Symmetry Breaking (EWSB)

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}\partial_{\mu}H\partial^{\mu}H + \frac{1}{2}\partial_{\mu}\chi\partial^{\mu}\chi + \frac{1}{2}(2e^{2}v^{2})A_{\mu}A^{\mu} + \sqrt{2}evA^{\mu}\partial_{\mu}\chi - eA^{\mu}(\chi\partial_{\mu}H + H\partial_{\mu}\chi) + \frac{1}{2}e^{2}A_{\mu}A^{\mu}(H^{2} + \chi^{2} - 2\sqrt{2}vH) - \frac{1}{2}(-2\mu^{2})H^{2} - \sqrt{2}\lambda vH(H^{2} + \chi^{2}) - \frac{\lambda}{4}(H^{2} + \chi^{2})^{2} + const.$$

\triangleright The theory has now

- $\bullet\,$ a photon of mass $M_A^2=2e^2v^2$
- a scalar field H with $M_{H}^{2}=-2\mu^{2}>0$
- a massless scalar field χ (Goldstone boson)
- \triangleright Mixed $A \chi$ propagator: can be removed by a gauge transformation

$$A_{\mu} o A_{\mu} + rac{1}{\sqrt{2}ev} \partial_{\mu} \chi$$
 and $\phi o e^{i rac{\chi}{\sqrt{2}v}} \phi$ (unitary gauge)

 \rightsquigarrow the χ field has been absorbed by a redefinition of A (jargon: χ has been "eaten" to give the photon mass)

▷ Degrees of freedom:

before symmetry breaking: massles gauge boson (2 dof) and complex scalar field (2 dof) after symmetry breaking: massive gauge boson (3 dof) and physical scalar (1 dof)

Spontaneously Broken Gauge Symmetries

- In spontaneously broken gauge theories the Goldstone bosons do not appear. They are would-be Goldstone bosons. After spontaneous symmetry breaking they are directly absorbed in the longitudinal degrees of freedom of the massive gauge bosons.
- \triangleright For gauge theories we have:
 - N = Dimension of the algebra of the symmetry group of the full Lagrangian.
 - M = Dimension of the algebra of the group, under which the vacuum after spontaneous symmetry breaking is invariant.
 - n =Number of scalar fields.

There are M massless vector fields. (M is the dimension of the symmetry of the vacuum.) There are N - M massive vector fields. (N - M is the number of broken generators.) There are n - (N - M) scalar Higgs fields. \bullet Add complex Higgs doublet to ${\cal L}$

$$\Phi = \left(egin{array}{c} \phi^+ \ \phi^0 \end{array}
ight) \hspace{0.5cm} ext{with} \hspace{0.5cm} < \Phi > = rac{1}{\sqrt{2}} \left(egin{array}{c} 0 \ v \end{array}
ight) \hspace{0.5cm} ext{and} \hspace{0.5cm} v = 246 ext{ GeV}$$

- Lagrangian of the Higgs doublet
 - $\mathcal{L}_{\Phi} = |D_{\mu}\Phi|^2 V(\Phi)$
- The Higgs potential:

$$V(\Phi) = \lambda [\Phi^{\dagger} \Phi - \frac{v^2}{2}]^2$$

The minimum of the potential is at v = 246 GeV \rightsquigarrow spontaneous symmetry breaking (SSB)



• Higgs field in the unitary gauge

$$\begin{split} \Phi &= \frac{1}{\sqrt{2}} \begin{pmatrix} 0\\ v+H \end{pmatrix} \Rightarrow \\ V(H) &= \frac{1}{2} M_H^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4 \end{split}$$

• \Rightarrow Higgs mass and self-couplings:

${\cal H}$ iggs boson mass	$M_H = \sqrt{2\lambda}v$
${\cal T}$ rilinear coupling [units $\lambda_0=33.8$ GeV]	$\lambda_{HHH} = 3 \frac{M_H^2}{M_Z^2}$
${\cal Q}$ artic coupling [units λ_0^2]	$\lambda_{HHHH} = 3 \frac{M_H^2}{M_Z^4}$

Higgs self-couplings in the SM uniquely determined by the Higgs mass!

• Gauge boson masses from

 $\mathcal{L}_{\Phi}^{\mathsf{kin}} = |D_{\mu}\Phi|^{2} \quad \text{with the covariant derivative} \quad iD_{\mu} = i\partial_{\mu} - \frac{g}{2}\vec{\tau}\vec{W}_{\mu} - \frac{g'}{2}YB_{\mu}$ $\vec{\tau}^{T} = (\tau_{1}, \tau_{2}, \tau_{3}), \qquad \tau^{i} = \mathsf{Pauli matrices}$ $\vec{W}_{\mu}^{T} = (W_{\mu}^{1}, W_{\mu}^{2}, W_{\mu}^{3}), B_{\mu} \quad SU(2), U(1) \text{ gauge fields} \quad g, g' \quad \mathsf{gauge couplings}$

Expansion of $\Phi = (\phi^+, \phi^0)^T$ about its vacuum expectation value $\Phi \to (0, \frac{1}{\sqrt{2}}[v+H])^T \Rightarrow$ we get for the covariant derivative in the unitary gauge

$$D_{\mu}\Phi = \frac{1}{\sqrt{2}} \left(\partial_{\mu} + i\frac{g}{2} \begin{pmatrix} W_{\mu}^{3} & \sqrt{2}W_{\mu}^{-} \\ \sqrt{2}W_{\mu}^{+} & -W_{\mu}^{3} \end{pmatrix} + i\frac{g'}{2}B_{\mu} \right) \begin{pmatrix} 0 \\ v + H \end{pmatrix}$$

with $W^\pm_\mu = W^1_\mu \pm i W^2_\mu$

leading to

$$|D_{\mu}\Phi|^{2} = \frac{1}{2}(\partial_{\mu}H)^{2} + \frac{g^{2}v^{2}}{4}W^{+\mu}W_{\mu}^{-} + \frac{v^{2}}{8}(gW_{\mu}^{3} - g'B_{\mu})^{2} + \text{ interaction terms}$$

 \Rightarrow massive gauge boson masses:

$$\begin{split} W^\pm_\mu \qquad \text{and} \quad Z_\mu = \frac{1}{\sqrt{g^2 + g'^2}} (g W^3_\mu - g' B_\mu) \\ \text{with masses} \quad M^\pm_W = \frac{1}{2} g v \quad \text{and} \quad M_Z = \frac{1}{2} \sqrt{g^2 + g'^2} v \qquad \text{with v=246 GeV} \end{split}$$

Orthogonal superposition to Z:

massless photon
$$A_{\mu}=\frac{1}{\sqrt{g^2+g'^2}}(g'W_{\mu}^3+gB_{\mu})$$

introducing the electroweak mixing angle θ_W we have

$$\sin \theta_W = \frac{g'}{\sqrt{g^2 + g'^2}}$$
 and $\cos \theta_W = \frac{g}{\sqrt{g^2 + g'^2}}$
so that $g' = g \tan \theta_W$ and $M_W = M_Z \cos \theta_W$

$\mathcal{T}he \ \mathcal{SM} \ \mathcal{H}iggs \ \mathcal{S}ector$

- Fermion masses: generated through the Yukawa interactions $(-h_e \bar{L}_L e_R \phi^0 + h.c.);$ $(L_L = (\nu_L, e_L)^T);$
 - e.g. for electrons (after expansion about vacuum expectation value (VEV) v, $\phi^0=1/\sqrt{2}(v+H)$)

$$\mathcal{L}_{\mathsf{Yuk}}^{e} = -\frac{h_{e}}{\sqrt{2}} \left(\begin{array}{c} \bar{\nu}_{L} \\ \bar{e}_{L} \end{array} \right)^{T} \left(\begin{array}{c} 0 \\ v + H \end{array} \right) e_{R} + \mathsf{h.c.}$$

\rightsquigarrow electron mass term

$$\mathcal{L}^{e}_{\mathsf{Yuk,mass}} = -\frac{h_e v}{\sqrt{2}} (\bar{e}_L e_R + \bar{e}_R e_L) = -\frac{h_e v}{\sqrt{2}} \bar{e} e \equiv -m_e \bar{e} e \qquad e_{L,R} = \frac{(\mathbb{I} \mp \gamma_5)}{2} e$$

The Yukawa coupling h_e is related to the electron mass by

$$h_e = g \frac{m_e}{\sqrt{2}M_W} \qquad \qquad M_W = \frac{gv}{2}$$

We also have an interaction between the electron and the Higgs boson

$$\mathcal{L}_{\text{int}} = -g \frac{m_e}{2M_W} H \bar{e} e$$

• Quark masses also generated through the Yukawa interactions

$$\mathcal{L}_{\mathsf{Yuk}}^{q} = -(\bar{u}_{R}, \bar{c}_{R}, \bar{t}_{R}) \begin{pmatrix} h_{u} & & \\ & h_{c} & \\ & & h_{t} \end{pmatrix} \begin{bmatrix} \phi^{0} \begin{pmatrix} u_{L} \\ c_{L} \\ t_{L} \end{pmatrix} - \phi^{+} V \begin{pmatrix} d_{L} \\ s_{L} \\ b_{L} \end{pmatrix} \end{bmatrix}$$

$$-(\bar{d}_{R}, \bar{s}_{R}, \bar{b}_{R}) \begin{pmatrix} h_{d} & & \\ & h_{s} & \\ & & h_{b} \end{pmatrix} \begin{bmatrix} \phi^{0} \begin{pmatrix} d_{L} \\ s_{L} \\ b_{L} \end{pmatrix} - \phi^{-} V^{\dagger} \begin{pmatrix} u_{L} \\ c_{L} \\ t_{L} \end{pmatrix} \end{bmatrix} + h.c.$$

V: Cabibbo-Kobayashi-Maskawa (CKM) matrix

Expansion about VEV \rightsquigarrow

$$\mathcal{L}_{mass}^{q} = \underbrace{-\frac{h_{d}v}{\sqrt{2}}\bar{d}_{L}d_{R} + h.c.}_{\text{d-quark mass}} \underbrace{-\frac{h_{u}v}{\sqrt{2}}\bar{u}_{L}u_{R} + h.c.}_{\text{u-quark mass}}$$

$$\text{u-quark mass}$$

$$\text{wasses:} \ m_{d} = \frac{h_{d}}{\sqrt{2}}v = \sqrt{2}\frac{h_{d}M_{W}}{g} \quad \text{and} \quad m_{u} = \frac{h_{u}}{\sqrt{2}}v = \sqrt{2}\frac{h_{u}M_{W}}{g}$$

 \rightarrow Interactions between the quarks and the Higgs boson: $\mathcal{L}_{int} = -g \frac{m_u}{2M_W} \bar{u} H u - g \frac{m_d}{2M_W} \bar{d} H d$

• The Lagrangian of the SM with one family is schematically

 $\mathcal{L}_{SM,1} = \sum_{\text{gauge bosons}} -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \sum_{\text{fermions}} i \bar{\psi} \gamma^{\mu} D_{\mu} \psi + \mathcal{L}_{\text{Yuk}} + |D_{\mu} \phi|^2 - V(\phi)$ where

 $F_{\mu\nu} = -\frac{1}{ig} [D_{\mu}, D_{\nu}] \qquad D_{\mu} = \partial_{\mu} + i \frac{g}{2} \tau^{i} W^{i}_{\mu} + i g' Y B_{\mu} + i \frac{g_{S}}{2} T^{a} G^{a}_{\mu}$

The term $F_{\mu\nu}F^{\mu\nu} \rightsquigarrow$ interactions among the gauge bosons, e.g. $g\epsilon_{ijk}(\partial_{\mu}W^{i}_{\nu})W^{\mu j}W^{\nu k} - \frac{1}{4}g^{2}\epsilon_{ijk}\epsilon_{ilm}W^{j}_{\mu}W^{k}_{\nu}W^{\mu l}W^{\nu m}$

The term $i\bar{\psi}\gamma^{\mu}D_{\mu}\psi \rightsquigarrow$ interactions among the fermions and gauge bosons, e.g. $(L_L = (\nu_L, e_L)^T)$

$$i\bar{L}_{L}^{T}\gamma^{\mu}D_{\mu}L_{L} + i\bar{e}_{R}\gamma^{\mu}D_{\mu}e_{R}$$

$$= -\frac{g}{2\sqrt{2}}\bar{\nu}\gamma^{\mu}(1-\gamma_{5})eW_{\mu}^{-} + \text{h.c.} + \overbrace{g\sin\theta_{W}}^{\equiv e}\bar{e}\gamma^{\mu}eA_{\mu}$$

$$-\frac{g}{4\cos\theta_{W}}\bar{\nu}\gamma^{\mu}(1-\gamma_{5})\nu Z_{\mu} + \frac{g}{4\cos\theta_{W}}\bar{e}(\gamma^{\mu}(1-\gamma_{5}) - 4\sin^{2}\theta_{W}\gamma^{\mu})eZ_{\mu}$$

$\mathcal{T}he \ \mathcal{S}tandard \ \mathcal{M}odel \ with \ one \ \mathcal{F}amily$

The free parameters of the $SU(2) \times U(1)$ part with one generation of leptons are

- \vartriangleright the two gauge couplings for the SU(2) and U(1) gauge groups, g and g'
- \vartriangleright the two parameters μ and λ in the scalar potential $V(\phi)$
- \triangleright the Yukawa couplings h_f

It is convenient to replace these parameters by parameters which can be measured accurately, e.g.

$$\{g, g', \lambda, v, h_f\} \rightarrow \{\alpha, \sin \theta_W, G_F, M_Z, m_f\}$$

where at Born level

$$\tan \theta_W = \frac{g'}{g} \qquad \alpha = \frac{g^2 \sin^2 \theta_W}{4\pi} \qquad M_H^2 = 2\lambda v^2$$
$$M_Z^2 = \frac{(g^2 + g'^2)v^2}{4} \qquad m_f = \frac{h_f v}{\sqrt{2}}$$

The values of other observables are predicted

$$\begin{split} M_W &= M_Z \cos \theta_W \quad , \quad A_{LR} = \frac{(-\frac{1}{2} + s_{eff}^2)^2 - s_{eff}^4}{(-\frac{1}{2} + s_{eff}^2)^2 + s_{eff}^4} \quad , \quad s_{eff}^2 = s_W^2 = \frac{g'^2}{g^2 + g'^2} \\ \Gamma(Z \to l^+ l^-) &= \frac{\sqrt{2}G_F}{6\pi} \, m_Z^3 \left(g_L^2 + g_R^2 \right) \quad , \quad \text{where} \quad g_L = -\frac{1}{2} + s_W^2 \, , \ g_R = s_W^2 \end{split}$$

Additional generations introduce more fermion masses and mixing angles.

$\mathcal{T}he \ \mathcal{S}tandard \ \mathcal{M}odel \ with \ one \ \mathcal{F}amily$

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$$M_Z^2 = \frac{(g^2 + g'^2)v^2}{4} \qquad m_f = \frac{h_f v}{\sqrt{2}}$$

The values of other observables are predicted

$$M_W = \frac{\sqrt{2\pi\alpha G_F^{-1}}}{1 - \sqrt{1 - 4\pi\alpha/(\sqrt{2}G_F M_Z^2)}} , \quad s_{eff}^2 = \frac{1}{2} - \sqrt{1/4 - \pi\alpha/(\sqrt{2}G_F M_Z^2)}$$
$$\Gamma(Z \to l^+ l^-) = \frac{\sqrt{2}G_F M_Z^3}{12\pi} \left(\left(\frac{1}{2} - \sqrt{1 - 4\pi\alpha/(\sqrt{2}G_F M_Z^2)} \right)^2 + \frac{1}{4} \right)$$

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$\mathcal{H} ow \ to \ \mathcal{V} erify \ the \ \mathcal{H} iggs \ \mathcal{M} echanism?$

- Higgs Mechanism: There is a Higgs Particle!
- Verification: First step: Production of the Higgs boson



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$\mathcal{LHC} \ \mathcal{D}iscovery \ of \ \mathcal{N}ew \ \mathcal{S}calar \ \mathcal{P}article$

ATLAS-CONF-2013-12

CMS-PAS-HIG-13-002



• 4 July 2012: CERN announces discovery of new scalar Higgs-like particle!



Higgs-Groupies queueing up in front of CERN audimax

• 4 July 2012: CERN announces discovery of new scalar Higgs-like particle!



Two electroweak symmetry breaking heroes



Crowd listening announcement at ICHEP 2012 in Melbourne



At the university of Tokyo
$\mathcal{D}iscovery \text{ of } \mathcal{N}ew \text{ Scalar } \mathcal{P}article$



At Fermilab

$\mathcal{D}iscovery \text{ of } \mathcal{N}ew \text{ Scalar } \mathcal{P}article$



At DESY, Hamburg

\mathcal{N} obel \mathcal{P} rize in \mathcal{P} hysics 2013



\mathcal{N} obel \mathcal{P} rize in \mathcal{P} hysics 2013



 $\ensuremath{\mathcal{B}}$ The production of a new particle with mass $M\approx 125~{\rm GeV}$

 \mathscr{B} Is it *the* Standard Model *Higgs* boson? \Longrightarrow



$\mathcal{E} x perimental \ \mathcal{V} erification \ of \ the \ \mathcal{H} iggs \ \mathcal{M} echanism$

Higgs mechanism:

Creation of particle masses without violating gauge symmetries



 $\begin{array}{l} \mathcal{H} \text{iggs } \mathcal{B} \text{oson } \mathcal{P} \text{roduction} \\ \text{at the } \mathcal{LHC} \end{array}$

Higgs boson production in the SM

- Gluon Fusion
 - $pp \to gg \to H$





$$pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + H$$



• Higgs-strahlung

 $pp \to W^*/Z^* \to W/Z + H$



• Associated Production

 $pp \rightarrow t\bar{t} + H$



Higgs boson production

- Gluon Gluon Fusion Room for New Physics! W/Z Fusion
 - $pp \to gg \to H$



• W/Z Fusion $pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + H$



• Higgs-strahlung



• Associated production with $t\bar{t}$ $pp \rightarrow t\bar{t} + H$



\mathcal{SM} $\mathcal{H}iggs$ $\mathcal{B}oson$ $\mathcal{P}roduction$ at the \mathcal{LHC}



LHC Higgs XS WG, arXiv:1101.0593

M.Mühlleitner, July, 7-9, 2014, European Summer School, Strasbourg

$\mathcal{LHC} \ \mathcal{H}iggs \ \mathcal{C}ross \ \mathcal{S}ection \ \mathcal{W}orking \ \mathcal{G}roup$

- ◇ "Handbook of LHC Higgs cross sections: 1. Inclusive observables." arXiv:1101.0593
- ◇ provide best theory prediction for Higgs cross sections and branching ratios (SM and MSSM)
- ◇ provide theoretical uncertainties on these quantities
- ◊ give precise common inputs
- ◊ inclusive cross sections (now also distributions (2./1201.3084) and Higgs properties (3./1307.1347))
- https://twiki.cern.ch/twiki/bin/view/LHCPhysics/Cross Sections

 $\mathcal{M} \text{ini-} \mathcal{P} \text{rimer on} \\ \mathcal{S} \text{cattering } \mathcal{P} \text{rocesses at the } \mathcal{LHC} \\ \end{array}$

Scattering processes at hadron colliders

- Connect incoming quarks, gluons with colliding protons outgoing particles with observed hadronic jets
- Scattering processes at high-energy hadron colliders: \rightarrow hard \rightarrow soft \leftarrow QCD
- Hard processes (e.g. Higgs boson or high- p_T jet production): perturbation theory
- Soft processes (e.g. total cross section, underlying event etc.) non-perturbative QCD effects

Factorisation theorem of the QCD

Partonic cross sections have collinear divergences in the hadronic initial state, which factorise universally (i.e. independent of the process) from the hard scattering process and can be absorbed in the renormalized parton densities of the initial state. These renormalized parton densities are solutions of the Altarelli-Parisi equations. • Master Formula $pp \rightarrow X$: QCD factorization

 $\sigma_{AB} = \sum_{ab} \int dx_1 dx_2 f_{a/A}(x_1, \mu_F^2) f_{b/B}(x_2, \mu_F^2) \hat{\sigma}_{ab \to X}$

A = B = p und a = b = q/g

• Partonic cross section $\hat{\sigma}$:

 \triangleright Partons of the incoming hadrons interact at short distance Example Drell-Yan process: $\hat{\sigma}(q\bar{q} \rightarrow l^+ l^-)$



• Parton distribution functions (pdf) $f_{a/A}(x_1, \mu_F^2), f_{b/B}(x_2, \mu_F^2)$

 $\triangleright x_1 = 2E_a/\sqrt{S}, x_2 = 2E_b/\sqrt{S}$ momentum fraction carried by the incoming quarks, gluons $\triangleright \mu_F^2$ factorization scale (separates short- and long-distance physics)

pdf's extracted from deep-inelastic scattering

Scattering processes at hadron colliders

• General process $\sigma(pp o X)$

 $\sigma_{pp\to X} = \sum_{a,b,k} f_{a/p}(\mu_F^2) \otimes f_{b/p}(\mu_F^2) \otimes \hat{\sigma}_{ab\to k}(\alpha_s(\mu_R^2), \mu_R^2) \otimes D_{k\to X}(\mu_F^2)$

• Partonic cross section $\hat{\sigma}_{ab \rightarrow k}$

calculable with perturbation theory in powers of α_s $\hat{\sigma}_{ab \to k} = [\hat{\sigma}_0 + \alpha_s(\mu_R^2)\hat{\sigma}_1 + \alpha_s^2(\mu_R^2)\hat{\sigma}_2 + ...]_{ab \to k}$

- Parton luminosity $f_{a/p}(\mu_F^2) \otimes f_{b/p}(\mu_F^2)$ proton: very complicated multi-particle bound state
- Final state X: hadrons, mesons, jets, ...
 - \triangleright fragmentation function $D_{k \to X}(\mu_F^2)$ or jet algorithm
 - ▷ interface with showering-algorithms (Monte Carlo)



Example Drell-Yan Process

• Drell-Yan Process



parton process

- Cross section: $\sigma(pp \to l^+l^-) = \sum_q \int dx_1 dx_2 \ f_q(x_1) \ f_{\bar{q}}(x_2) \ \hat{\sigma}(q\bar{q} \to l^+l^-)$
- $ightarrow f_{q/\bar{q}}(x)dx$: probability to find (anti)quark with momenum fraction xprocess independent, measured in DIS
- $\triangleright \hat{\sigma}(q\bar{q} \rightarrow l^+l^-)$: hard scattering cross section

calculable in perturbation theory

Example Drell-Yan Process

• Factorisation not trivial beyond leading order

virtual corrections

real corrections





▷ UV divergences▷ IR divergences

> IR divergences> collinear divergences

UV divergences \rightarrow renormalization $\alpha_S(\mu_R)$ etc.

IR divergences \rightarrow cancel between virtual and real correction (Kinoshita-Lee-Nauenberg theorem) collinear initial state divergences \rightarrow absorbed in pdf's

Example Drell-Yan Process

• Example: initial state collinear singularity



process independent divergence in $\int dk_T^2$ as $k_T^2 \rightarrow 0$ \rightsquigarrow absorb singularity in parton densities

 $f_q(x,\mu_F) = f_q(x) + (\text{divergent part of } \int_0^{\mu_F^2} dk_T^2)$

• Hadron collider cross section

 $\sigma = \int dx_1 f_i(x_1, \mu_F) \int dx_2 f_j(x_2, \mu_F) \times \sum_n \alpha_S^n(\mu_R) C_n(\mu_R, \mu_F) + \mathcal{O}(\Lambda_{QCD}/Q)$

Altarelli, Ellis, Martinell; Collins, Soper, Sterman; ...

• Interactions between spectator partons ~> underlying event and/or multiple hard scattering

${\cal H}igher \; {\cal O}rder \; {\cal C}orrections$

LHC is a proton-proton machine processes depend on strong coupling constant $\alpha_s \rightsquigarrow$ higher order corrections can be substantial \rightsquigarrow are important

Precision calculations needed for signal and background processes

- $\diamond~$ Higgs discovery in WW decay \leftarrow no reconstruction of the mass peak possible
- ◇ reliable extraction of the discovery/exclusion significances
- $\diamond\,$ precise measurement of the Higgs couplings

٥ ...

\Rightarrow

- \triangleright test of the Higgs mechanism
- ▷ discrimination between SM and SM extensions (e.g. SUSY)

$\mathcal{H}iggs \; \mathcal{B}oson \; \mathcal{P}roduction \; in \; \mathcal{G}luon \; \mathcal{F}usion$

(i) Dominant: Gluon Fusion $pp \rightarrow gg \rightarrow H$

Georgi et al; Gamberini et al



• Loop-induced process

- * dominant contribution: Q = top Quark
- * subleading contribution: Q = bottom Quark (< 10%)
- Strong dependence on factorization and renormalization scales (100%)

 whigher order corrections are very important
- New Physics: process is sensitive to new heavy particles in the loop (no decoupling)

$\mathcal{H}igher \ \mathcal{O}rder \ \mathcal{C}orrections$

• Effective Theory for $m_t \rightarrow \infty$, $m_b \rightarrow 0$ simplifies loop calculations considerably physical picture: long-range gluon interaction does not resolve Higgs production \rightsquigarrow effective Higgs-gluon-gluon coupling



- Local effective interaction: $\mathcal{L}_{Hgg} = \frac{\alpha_s}{12\pi} G^a_{\mu\nu} G^{a\,\mu\nu} \frac{H}{v} (1 + \frac{11\alpha_s}{4\pi} + ...)$
- NLO correction with full mass dependence: increase σ by up to $\sim 100\%$

Spira,Djouadi,Graudenz,Zerwas Dawson;Kauffman,Schaffer

• Typical diagrams contributing to virtual and real corrections including full mass dependence



Status of Higher Order Corrections

QCD corrections

- \triangleright complete NLO: increase σ by \sim 80-100%
- \triangleright SM: limit $M_{\Phi} \ll m_t$ approximation \sim 20-30%
- \triangleright NNLO @ $M_{\Phi} \ll m_t \Rightarrow$ further increase by 20-30%
- $\triangleright~$ Estimate of NNNLO effects @ $M_{\Phi} \ll m_t \rightsquigarrow$ scale stabilisation scale dependence: $\Delta \lesssim 10-15\%$

Spira, Djouadi, Graudenz, Zerwas Dawson; Kauffman, Schaffer

Krämer, Laenen, Spira

Harlander,Kilgore Anastasiou,Melnikov Ravindran,Smith,van Neerven Moch,Vogt Ravindran

$gg \to H$ at \mathcal{NNLO} and beyond



M.Mühlleitner, July, 7-9, 2014, European Summer School, Strasbourg

$\mathcal{S} tatus of \ \mathcal{H} igher \ \mathcal{O} rder \ \mathcal{C} orrections$

QCD corrections

- \triangleright complete NLO: increase σ by \sim 80-100%
- \triangleright SM: limit $M_{\Phi} \ll m_t$ approximation \sim 20-30%
- \triangleright NNLO @ $M_{\Phi} \ll m_t \Rightarrow$ further increase by 20-30%
- > NNNLO effects estimate @ $M_{\Phi} \ll m_t \rightsquigarrow$ scale stabl. scale dependence: $\Delta \lesssim 10 - 15\%$
- \triangleright NNLL resummation: $\sim 6 9\%$
- \triangleright leading soft contribution at N³LO in limit $m_t \to \infty$
- ▷ NNLO mass effects (t loops) for $M_H \leq 300 \text{ GeV} \Rightarrow \mathcal{O}(0.5\%)$
- \triangleright NLO electroweak corrections $\sim \mathcal{O}(5\%)$ (SM)
- \triangleright mixed QCD and EW corrections
- ho NLO for $H+{
 m jet}~\lesssim 1\%$
- \triangleright Steps towards N³LO in gluon fusion

Spira, Djouadi, Graudenz, Zerwas Dawson; Kauffman, Schaffer

Krämer, Laenen, Spira

Harlander,Kilgore Anastasiou,Melnikov Ravindran,Smith,van Neerven Moch,Vogt Ravindran

Catani,de Florian,Grazzini,Nason Moch,Vogt; Laenen,Magnea; Idilbi eal

Ravindran,Smith,van Nerven; Ahrens eal

Harlander,Ozeren;Pak,Rogal,Steinhauser; Marzani et al.

Aglietti et al.;Degrassi,Maltoni; Actis et al

Anastasiou, Boughezal, Petriello

Keung, Petriello; Brein

Chetyrkin eal;Schröder,Steinhauser;Baikov eal; Gehrmann eal;Lee eal;Anastasiou eal; Höschele eal; Bühler,Lazopoulos;Boughezal eal;Ball eal;Moch,Vogt (ii) W/Z Boson Fusion: $pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + H$



Cahn,Dawson Hikasa Altarelli,Mele,Pitolli

Contribution to $H\to\gamma\gamma$ discovery contour

Important role in Higgs coupling determination at the LHC Dührssen et al.; Hankele et al. Rauch et al.; Englert et al.

Typical signature: 2 hard jets with large rapidity interval, no hadronic activity in between

• VBF cuts and background suppression:

* 2 hard tagging jets demanded: $p_{T_j} > 20~{\rm GeV}$, $|y_j| < 4.5$

* tagging jets forward-backward directed: $\Delta y_{jj} > 4$, $y_{j1} \cdot y_{j2} < 0$

Status of Higher Order Corrections to Higgs+2jets Production

\triangleright	NLO QCD corrections to		
	total rate	\sim 5 to 10%	Han,Valencia,Willenbrock Spira; Djouadi,Spira
	Distributions	$\sim 20~\%$	Figy,Oleari,Zeppenfeld Berger,Campbell
	dominant NLO QCD to H+3j		Figy,Hankele,Zeppenfeld
\triangleright	NLO QCD corrections to		
	gluon-initiated channels		Campbell,Ellis,Zanderighi
	contribution to VBF $\sim 5\%$	scale uncert $\sim 35\%$	Nikitenko,Vázquez,Acosta
\triangleright	Matching with parton shower (POWHEG)		Nason,Oleari
\triangleright	Full EW & QCD corrections	$\sim 5\%$	Ciccolini,Denner,Dittmaier Figy,Palmer,Weiglein
\triangleright	One-loop interference effects in H+jj		Andersen, Binoth, Heinrich, Smillie Bredenstein, Hagiwara, Jäger
	between gg -initiated and VBF	below percent level	
	implemented in VBFNLO		Bredenstein, Hagiwara, Jäger
\triangleright	NNLO QCD effects in DIS-like approx	$\sim 1-2\%~~{\cal O}(M_W)$	Bolzoni, Maltoni, Moch, Zaro
\triangleright	Loop-induced VBF in gg scattering	impact $\sim 0.1\%$	Harlander, Vollinga, Weber

```
(iii) pp 
ightarrow q ar q 
ightarrow Z^*/W^* 
ightarrow Z/W + H
```



Glashow et al. Kunszt et al.

- Important production process at Tevatron
- LHC: contribution to $\Phi \rightarrow \gamma \gamma$ discovery contours
- NLO QCD Korrekturen $\sim +30\%$ (Drell-Yan) Han, Willenbrock

NNLO QCD Korrekturen $\sim +5-10\%$ Harlander, Kilgore Hamberg, Van Neerven, Matsuura Brein, Djouadi, Harlander

• Complete EW corrections $\sim -5-10\%$ Ciccolini, Dittmaier, Krämer

$WH: \mathcal{F}ully \mathcal{E}xclusive at \mathcal{NNLO} \mathsf{QCD}$

WH: fully exclusive at NNLO QCD

- finite width effects
- W boson leptonic decay w/ spin correlations
- Higgs decay into $b\bar{b}$



Ferrera, Grazzini, Tramontano '11

scale dep $\pm 13\%$ (NLO) $\rightarrow \pm 6\%$ (NNLO)

(iv) Higgs $tar{t}$ Production: $pp
ightarrow qar{q}/gg
ightarrow tar{t} + H$



Significant role for: $M_{H}^{SM} \lesssim 150 {\rm ~GeV}$

- $t ar{t} H o t ar{t} \gamma \gamma$ important contribution to $H o \gamma \gamma$ discovery contour
- $t\bar{t}H \rightarrow t\bar{t}b\bar{b}$ important at LHC \rightsquigarrow top Yukawa coupling
- NLO bkg $t\bar{t}b\bar{b}$, $t\bar{t}jj$ important

Gunion et al.; Drollinger et al.

Bredenstein, Denner, Dittmaier, Pozzorini; Bevilacqua, Czakon, Papadopoulos, Pittau, Worek

\mathcal{NLO} QCD Corrections to $t\bar{t}b\bar{b}+X$ at the \mathcal{LHC}

- $t\bar{t}b\bar{b}$ final states very important background to $t\bar{t}H$
- $t\bar{t}H$ discovery contour \leftarrow very good control of $t\bar{t}b\bar{b}$, $t\bar{t}+$ jets background necessary
- NLO QCD corrections to
 - $ightarrow t\bar{t}H$ Beenakker eal;Dawson eal $\sim +20\%$ $\Delta_{\rm theor} \sim 15\%$
 - $\triangleright t\bar{t}$ +jet Dittmaier,Uwer,Weinzierl
 - $rac{b}{b}t\bar{t} + jj$ Bevilacqua, Czakon, Papadopoulos, Worek
- NLO QCD corrections to $t\bar{t}b\bar{b}$

Bredenstein, Denner, Dittmaier, Pozzorini; Bevilacqua, Czakon, Papadopoulos, Pittau, Worek

First full NLO calculation for $2 \rightarrow 4$ process at a hadron collider

 Some generic hexagon diagrams to the virtual corrections



\mathcal{NLO} QCD Corrections to $t\bar{t}b\bar{b}+X$ at the \mathcal{LHC}



 \bullet reduction of scale dependence: LO 100 % \rightarrow NLO 20-30 %

• increased cross section: K factor ≈ 1.24

\mathcal{H} iggs \mathcal{B} oson \mathcal{D} ecays

• Higgs boson coupling ~ particle mass ~ most important decays: into heavy particles

Fermions

 $\begin{array}{ll} BR(H \to b\bar{b}) &\lesssim 85\% \\ BR(H \to \tau^+ \tau^-) &\lesssim 8\% \\ BR(H \to c\bar{c}) &\lesssim 4\% \\ BR(H \to t\bar{t}) &\lesssim 20\% \end{array}$

large QCD corrections, up to $\mathcal{O}(50\%)$

 $H - - - \bigvee_{f} f$

Braaten,Leveille; Sakai; Inami,Kubota; Drees,Hikasa; Gorishnii,Kataev,Larin,Surguladze; Kataev,Kim; Larin,van Ritbergen, Vermaseren; Chetyrkin,Kwiatkowski; Baikov,Chetyrkin,Kühn

Gauge bosons M_V^2 W^+, Z $BR(H \rightarrow W^+W^-)$ \lesssim 60 - 95% ψ $BR(H \rightarrow ZZ)$ \lesssim 30%H - - - 4EW corrections $\mathcal{O}(5 - 20\%)$ W^-, Z

Off-shell decays $H \to V^*V^* \to 4l$ important for $M_H = 125$ GeV PROPHECY4F for $H \to WW/ZZ \to 4f$ (complete QCD and EW NLO corrections)

Bredenstein, Denner, Dittmaier, Mück, Weber

$\mathcal{H}iggs \ \mathcal{B}oson \ \mathcal{D}ecays$

<u>Gluons</u>

$$BR(H \to gg) \lesssim 6\%$$

Loop-mediated decays, dominant contribution from top loops large QCD corrections, up to +70% at NLO; known up to $N^{3}LO$



Baikov, Chetyrkin;

Chetyrkin, Kniehl, Steinhauser; Krämer, Laenen, Spira; Schröder, Steinhauser; Chetyrkin, Kühn, Sturm; Inami eal; Djouadi, Graudenz, Spira, Zerwas; Dawson eal; Harlander, Steinhauser; Harlander, Hofmann

 $\frac{\gamma\gamma \text{ and } Z\gamma}{BR(H \to \gamma\gamma, Z\gamma)} \lesssim 2 \times 10^{-3}$

Loop-mediated decay via charged fermions and W bosons QCD corrections small

Djouadi,Graudenz,Spira,Zerwas; Melnikov,Spira,Yakovlev; Zheng,Wu Dawson,Kauffmann;Melnikov,Yakovlev; Inoue,Najima,Okada,Saito



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Higgs Boson Decays

Branching ratios LHC HIGGS XS WG 2010 LHC HIGGS XS WG 2010 E WW bb 77 gg 10⁻¹ $-\tau\tau$ 10 \overline{C} 1 10⁻² 10⁻¹ Ζγ γγ 10⁻² 10⁻³ 120 140 160 200 200 300 100 180 100 500 1000 M_H [GeV] M_{H} [GeV]

Higgs cxn working group

\mathcal{T} otal \mathcal{W} idth

Higgs Total Width $\Gamma_{H}\approx 4.4~{\rm MeV}$

• interference between Higgs signal $gg \to H \to \gamma\gamma$ and continuum $gg \to \gamma\gamma \rightsquigarrow$ Higgs mass shift

S.P.Martin '12,'13; Dixon,Li '13

• Off-shell $H \to Z^*Z^*$ production



Caola,Melnikov '13; Campbell,Ellis,Williams '13; Kauer,Passarino '12



Present Value - combined 4l and $2l2\nu$ final states

CMS Moriond '13 New!

 $\Gamma < 17$ MeV (35 MeV expected) $\,$ 95% CL $\,$

Projection to HL-LHC

dominated by systematics

e.g. $pp \rightarrow ZZ$ at NNLO QCD required, realistic target, see e.g.

Gehrmann, Tancredi, Weihs '13
LHC Higgs XS WG



Note: Decay into $\gamma\gamma$ is loop-mediated (also into $Z\gamma$ and gg): Room for New Physics!



- Combination of all production and decay channels: exploit data maximally
- Production: dominant process gluon fusion, followed by VBF
- Decay:
 - * Gold plated: ZZ (off-shell for $M_H = 125$ GeV) \rightsquigarrow clean 4l final state
 - * $\gamma\gamma$: small branching ratio, but clean final state
 - * WW: (off-shell for $M_H = 125$ GeV) missing energy in final state, exploit transverse mass
 - * $b\bar{b}$: large uncertainties due to large QCD background
 - * au au: large uncertainties, difficult to measure
- What experiment tells us: best fit values to signal rates

$$\mu = \frac{\sigma_{prod} \times BR(H \to XX)}{(\sigma_{prod} \times BR(H \to XX))_{SM}}$$

$\mathcal{LHC} \ \mathcal{D}iscovery \ of \ \mathcal{N}ew \ \mathcal{S}calar \ \mathcal{P}article$

ATLAS-CONF-2013-12

CMS-PAS-HIG-13-002



What \mathcal{E} xperiment tells us: \mathcal{B} est \mathcal{F} it \mathcal{V} alues of $\mu = (\sigma \times BR)/(\sigma \times BR)_{SM}$

CMS April 2014



What \mathcal{E} xperiment tells us: \mathcal{B} est \mathcal{F} it \mathcal{V} alues of $\mu = (\sigma \times BR)/(\sigma \times BR)_{SM}$



ATLAS-CONF-2014-009

$\mathcal{E} \textbf{x} perimental \ \mathcal{V} erification \ of \ the \ EWSB \ \mathcal{M} echanism$

EWSB mechanism:

Creation of particle masses without violating gauge principles



$\mathcal{D}etermination \ of \ the \ \mathcal{H}iggs \ \mathcal{B}oson \ \mathcal{C}ouplings$

Strategy

Combination of the production and decay channels \Rightarrow decay rates, absolute couplings



$\mathcal{D}etermination \ of \ the \ \mathcal{H}iggs \ \mathcal{B}oson \ \mathcal{C}ouplings$

Strategy

Combination of the production and decay channels \Rightarrow decay rates, absolute couplings

$$\sigma_{\mathsf{prod}}(H) \times \mathsf{BR}(H \to XX) \sim \Gamma_{\mathsf{prod}} \times \frac{\Gamma_{\mathsf{decay}}}{\Gamma_{\mathsf{tot}}}$$

Coupling measurement at the LHC

- * Determination of total width impossible w/o further assumptions
- * Not all final states are accessible
- $*\,\,\Rightarrow\, {\rm Only}$ ratios of couplings can be measured
- $*\,\Rightarrow$ Perform fits to reduced signal strengths μ

 $\mu = \frac{\sigma \times \mathsf{BR}}{(\sigma \times \mathsf{BR})_{\mathsf{SM}}}$

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Experimental Status: Couplings

CMS-PAS-HIG-13-005

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$\mathcal{T}\text{heoretical}\ \mathcal{A}\text{pproach to}\ \mathcal{C}\text{oupling}\ \mathcal{E}\text{xtraction}$

• Couplings extracted from $\mu = (\sigma \times BR)/(\sigma \times BR)_{SM}$ values provided by experiments

• Theoretical approach

- * Effective Lagrangian which defines the meaning of the couplings
- * Effective Lagrangian w/ modified Higgs couplings \rightarrow signal rates \rightarrow fit to experimental μ values

◊ For further work, see:

D.Carmi, A.Falkowski, E.Kuflik, T.Volansky; D.Carmi, A.Falkowski, E.Kuflik, T.Volansky, J.Zupan;
A.Azatov, R.Contino, J.Galloway; P.Giardino, K.Kannike, M.Raidal, A.Strumia;
J.Ellis, T.You; M.Klute, R.Lafaye, T.Plehn, M.Rauch, D.Zerwas; M.Montull, F.Riva;
I.Low, J.Lykken, G.Shaugnessy; T.Corbett, O.Eboli, J.González-Fraile, M.C. González-Garcia;
S. Banerjee, S. Mukhopadhyay, B. Mukhopadhyaya; Cao eal; T.Plehn, M. Rauch;
Baglio, Djouadi, Godbole; Bélanger, Dumon, Ellwanger, Gunion, Kraml; Buchalla, Cata, Krause;

\mathcal{N} on- \mathcal{L} inear \mathcal{E} ffective \mathcal{L} agrangian

 \diamond Field content: SM with scalar field h; SM: $\kappa_i = 1, \overline{\kappa}_i = 0$ Contino eal '10,'12; Azatov eal; Alonso eal; Brivio eal; Elias-Miró eal; Isidori eal; Buchalla eal

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h \ \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} - \kappa_{3} \left(\frac{m_{h}^{2}}{2v} \right) h^{3} - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + \kappa_{\psi} \frac{h}{v} + \ldots \right)$$
$$- M_{W}^{2} W_{\mu}^{+} W^{-\mu} \left(1 + 2\kappa_{W} \frac{h}{v} + \ldots \right) - \frac{1}{2} M_{Z}^{2} Z_{\mu} Z^{\mu} \left(1 + 2\kappa_{Z} \frac{h}{v} + \ldots \right) + \ldots$$
$$+ \left(\frac{\bar{\kappa}_{WW} \alpha}{\pi} W_{\mu\nu}^{+} W^{-\mu\nu} + \frac{\bar{\kappa}_{ZZ} \alpha}{2\pi} Z_{\mu\nu} Z^{\mu\nu} + \frac{\bar{\kappa}_{Z\gamma} \alpha}{\pi} Z_{\mu\nu} \gamma^{\mu\nu} + \frac{\bar{\kappa}_{\gamma} \alpha}{2\pi} \gamma_{\mu\nu} \gamma^{\mu\nu} + \frac{\bar{\kappa}_{g} \alpha_{s}}{12\pi} G_{\mu\nu}^{a} G^{a\mu\nu} \right) \frac{h}{v}$$
$$+ \left(\left(\bar{\kappa}_{W\partial W} W_{\nu}^{-} D_{\mu} W^{+\mu\nu} + h.c. \right) + \bar{\kappa}_{Z\partial Z} Z_{\nu} \partial_{\mu} Z^{\mu\nu} + \bar{\kappa}_{Z\partial\gamma} Z_{\nu} \partial_{\mu} \gamma^{\mu\nu} \right) \frac{h}{v} + \ldots$$

 \diamond **Remarks:** * Valid for *h* being singlet or doublet

* $\overline{\kappa}_{g,\gamma,Z\gamma}$ parametrize new physics in the hgg, $h\gamma\gamma$ and $hZ\gamma$ loop couplings

$\mathcal{I}s \text{ it the } \mathcal{SM} \text{ } \mathcal{H}iggs \text{ } \mathcal{B}oson? \text{ - } \mathcal{E}ffective \text{ } \mathcal{L}agrangian \text{ } \mathcal{A}pproach$

$$\mathcal{L} = \mathcal{L}_{h} - (M_{W}^{2}W_{\mu}^{+}W^{\mu-} + \frac{1}{2}M_{Z}^{2}Z_{\mu}Z^{\mu})[1 + 2\kappa_{V}\frac{h}{v} + \mathcal{O}(h^{2})] - m_{\psi_{i}}\bar{\psi}_{i}\psi_{i}[1 + \kappa_{F}\frac{h}{v} + \mathcal{O}(h^{2})] + \dots$$

- Extension of the SM Lagrangian by two parameters κ_V, κ_F ; SM: $(\kappa_V, \kappa_F) = (1, 1)$
- Modified decays rates: HDECAY: Djouadi, Spira, Kalinowski, MMM

$\mathcal{I}s \text{ it the } \mathcal{SM} \text{ } \mathcal{H}iggs \text{ } \mathcal{B}oson? \text{ - } \mathcal{E}ffective \text{ } \mathcal{L}agrangian \text{ } \mathcal{A}pproach$

$$\mathcal{L} = \mathcal{L}_{h} - (M_{W}^{2}W_{\mu}^{+}W^{\mu-} + \frac{1}{2}M_{Z}^{2}Z_{\mu}Z^{\mu})[1 + 2\kappa_{V}\frac{h}{v} + \mathcal{O}(h^{2})] - m_{\psi_{i}}\bar{\psi}_{i}\psi_{i}[1 + \kappa_{F}\frac{h}{v} + \mathcal{O}(h^{2})] + \dots$$

- Extension of the SM Lagrangian by two parameters κ_V, κ_F ; SM: $(\kappa_V, \kappa_F) = (1, 1)$
- Modified decays rates: HDECAY: Djouadi, Spira, Kalinowski, MMM

$$h \to \gamma \gamma: \qquad H \longrightarrow \kappa_F \qquad H \longrightarrow \kappa_V \qquad H \longrightarrow \kappa_V \qquad H \longrightarrow \kappa_V \qquad K_V \qquad H \longrightarrow \kappa_V \qquad K_V \qquad K_V$$

$\mathcal{I}s \text{ it the } \mathcal{SM} \text{ } \mathcal{H}iggs \text{ } \mathcal{B}oson? \text{ - } \mathcal{E}ffective \text{ } \mathcal{L}agrangian \text{ } \mathcal{A}pproach$

$$\mathcal{L} = \mathcal{L}_{h} - (M_{W}^{2}W_{\mu}^{+}W^{\mu-} + \frac{1}{2}M_{Z}^{2}Z_{\mu}Z^{\mu})[1 + 2\kappa_{V}\frac{h}{v} + \mathcal{O}(h^{2})] - m_{\psi_{i}}\bar{\psi}_{i}\psi_{i}[1 + \kappa_{F}\frac{h}{v} + \mathcal{O}(h^{2})] + \dots$$

- Extension of the SM Lagrangian by two parameters κ_V, κ_F ; SM: $(\kappa_V, \kappa_F) = (1, 1)$
- Modified decays rates: HDECAY: Djouadi, Spira, Kalinowski, MMM

Modified Higgs-gluon-gluon coupling:

- ▷ Coupling modifications affect Higgs signal but not background signal rates changed, but kinematics unaffected ⇒ Rescale SM searches
- > NNLO QCD corrections: not affected by modified Higgs couplings (not true for NLO EW)
- ▷ Rescaling Production (NNLO QCD)

▷ Rescaling - Decay

$$\frac{\Gamma(H \to f\bar{f})}{\Gamma(H \to f\bar{f})^{SM}} = \frac{\Gamma(H \to gg)}{\Gamma(H \to gg)^{SM}} = \kappa_F^2 \quad \frac{\Gamma(H \to VV)}{\Gamma(H \to VV)^{SM}} = \kappa_V^2 \quad \frac{\Gamma(H \to \gamma\gamma)}{\Gamma(H \to \gamma\gamma)^{SM}} = \frac{(\kappa_V J_\gamma - \kappa_F I_\gamma)^2}{(J_\gamma - I_\gamma)^2}$$

\mathcal{F} it to \mathcal{LHC} \mathcal{D} ata within SM $(a \equiv \kappa_V, c \equiv \kappa_F)$ - \mathcal{S} ummer 2012

 χ^2 fit to $\hat{\mu}_i \pm \sigma_i$ from 48 channels (ATLAS+CMS+Tevatron)

Espinosa, Grojean, MMM, Trott '12

M.Mühlleitner, July, 7-9, 2014, European Summer School, Strasbourg

${\mathcal F}$ it to ${\mathcal L}{\mathcal H}{\mathcal C}$ ${\mathcal D}$ ata within ${\sf SM}(\kappa_V,\kappa_F)$

• Best fit points

 $\diamond~{\rm Solution}~{\rm for}~\kappa_F<0$

$$\Gamma(H \to \gamma \gamma) = \frac{(\kappa_V J_\gamma - \kappa_F I_\gamma)^2}{(J_\gamma - I_\gamma)^2} \Gamma^{SM}(H \to \gamma \gamma)$$

Constructive interference for $\kappa_F < 0$.

• For further work, see:

D.Carmi, A.Falkowski, E.Kuflik, T.Volansky; D.Carmi, A.Falkowski, E.Kuflik, T.Volansky, J.Zupan;
A.Azatov, R.Contino, J.Galloway; P.Giardino, K.Kannike, M.Raidal, A.Strumia;
J.Ellis, T.You; M.Klute, R.Lafaye, T.Plehn, M.Rauch, D.Zerwas; M.Montull, F.Riva;
I.Low, J.Lykken, G.Shaugnessy; T.Corbett, O.Eboli, J.González-Fraile, M.C. González-Garcia;
S. Banerjee, S. Mukhopadhyay, B. Mukhopadhyaya; Cao eal; T.Plehn, M. Rauch;
Baglio, Djouadi, Godbole; Bélanger, Dumon, Ellwanger, Gunion, Kraml ...

Status: Coupling Scale Factor Measurements

CMS Collaboration

ATLAS-CONF-2014-009

$\mathcal{H}iggs \; \mathcal{B}oson \; \mathcal{Q}uantum \; \mathcal{N}umbers$

• Quantum numbers of the Higgs boson: $J^{PC} = D^{PC} + D^{PC}$ parity C charge conjugation

• Vast literature:

Miller eal; Plehn eal; Choi eal; Odagiri; Buszello eal; Ellis eal; Godbole eal; Kramer eal; Berge al; Hagiwara eal; Hankele eal; Gao eal; De Rujula eal; Christensen eal; Englert eal; De Sanctis eal; Bolognesi eal; Boughezal eal; Coleppa eal; Stolarski eal; Alves; Chen eal; Banerjee eal; Freitas, Schwaller; Modak eal; Frank eal; Djouadi eal; Artoisenet eal; Desai eal; Schlegel eal; de Aquino, Mawatari; ...

• Observation in $\gamma\gamma$: No spin 1 [Landau-Yang]; C=+1 [assuming charge invariance]

• Theoretical Tools:

- * helicity analyses
- * operator expansions

• Systematic analysis of production and decay processes

$\mathcal{H}iggs \; \mathcal{B}oson \; \mathcal{Q}uantum \; \mathcal{N}umbers$

• Systematic analysis of production and decay processes

* V^*V decays	Buszello,Fleck,Marquard,van der Bij;Choi eal; Gao eal; De Rujula eal; Bolognesi eal; Englert eal; Boughezal eal
* $\gamma\gamma$ decays	Ellis, Hwang; Alves; Choi eal
* $Z\gamma$ decays	Stolarski, Vega-Morales; Choi eal
* CP-violating decays	Soni, Xu; Chang eal; Godbole eal; Nelson; De Rujula eal: Buszello eal; Freitas, Schwaller
* Fermionic decays (\rightarrow CP violation)	Kramer eal; Berge eal; Banerjee eal
* Production in gluon fusion, in vector boson fusion	Plehn eal; Hagiwara eal; Buszello, Marquard; Hankele eal; Campanario eal; Del Duca eal; Frank eal
* Production in Higgs-strahlung	Miller eal; Ellis eal; Englert eal; Frank eal; Djouadi eal; Christensen eal
* Hadronic event shapes	Englert eal
* Correlations among branching ratios	Coleppa eal; Ellis eal

(I) Angular \mathcal{D} istributions/ \mathcal{T} hresholds in $H \to VV^* \to 4\ell$

 \diamond Determination of spin and parity in

 $H \to ZZ^{(*)} \to (f_1\bar{f}_1)(f_2\bar{f}_2)$

in H c.m. frame

♦ Helicity methods to generalize to arbitrary spin and parity

$$\langle Z(\lambda_1) Z(\lambda_2) | H_{\mathcal{J}}(m) \rangle = \mathcal{T}_{\lambda_1 \lambda_2} d_{m,\lambda_1 - \lambda_2}^{\mathcal{J}}(\Theta) e^{-i(m - \lambda_1 + \lambda_2)\varphi}$$

 \diamond General tensor for HZZ vertex for each $\mathcal{J}^{\mathcal{P}}$

 $\mathcal{J} = T_{\mu\nu\beta_1\dots\beta_{\mathcal{J}}} \epsilon^* (Z_1)^{\mu} \epsilon^* (Z_2)^{\nu} \epsilon (H)^{\beta_1\dots\beta_{\mathcal{J}}}$

\mathcal{D} ifferential \mathcal{D} istributions \mathcal{P} ure- \mathcal{S} pin/ \mathcal{P} arity \mathcal{U} npolarized \mathcal{B} oson H^J

◇ Double polar angular distribution (CP-invariant theory)

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\cos\theta_1 d\cos\theta_2} = \left[\sin^2\theta_1 \sin^2\theta_2 |\mathcal{T}_{00}|^2 + \frac{1}{2} (1 + \cos^2\theta_1) (1 + \cos^2\theta_2) \left[|\mathcal{T}_{11}|^2 + |\mathcal{T}_{1,-1}|^2 \right] \right] \\ + (1 + \cos^2\theta_1) \sin^2\theta_2 |\mathcal{T}_{10}|^2 + \sin^2\theta_1 (1 + \cos^2\theta_2) |\mathcal{T}_{01}|^2 \right] / \mathcal{N}$$

 $\mathcal{N} = (16/9) \sum |\mathcal{T}_{\lambda\lambda'}|^2$ – normalization

◊ Azimuthal angular distribution (CP-invariant theory)

$$\frac{1}{\Gamma'}\frac{d\Gamma'}{d\phi} = \frac{1}{2\pi} \left[1 + |\zeta_1|\cos 2\phi\right]$$

 $|\zeta_1| = |\mathcal{T}_{11}|^2 / \left[2\sum |\mathcal{T}_{\lambda\lambda'}|^2\right]$

suppressing terms quadratic in $\eta_i = 2v_i a_i / (v_i^2 + a_i^2) \sim 0.02$, v_i, a_i electroweak fermion f_i charges

$\mathcal{D}etermination \ of \ \mathcal{S}pin \ and \ \mathcal{P}arity \ - \ \mathcal{G}eneral \ \mathcal{C}ase$

• $M_H < 2M_Z$:	$d\Gamma/dM$	$\mathcal{J}^2_* \sim eta$ for $\mathcal{J}^\mathcal{P} = 0^+$	
$\diamond d\Gamma/dM_*^2$	rules out	$\mathcal{J}^{\mathcal{P}} = 0^{-}, 1^{-}, 2^{-}, 3^{\pm}, 4^{\pm}$	
$\diamond d\Gamma/dM_*^2$	and no	$[1+\cos^2\theta_1]\sin^2\theta_2$	
		$[1+\cos^2\theta_2]\sin^2\theta_1$	rules out $\mathcal{J}^{\mathcal{P}}=1^+,2^+$

$ullet \ M_H > 2M_Z$:

 $\begin{aligned} \diamond \text{ odd normality:} \quad \mathcal{J}^{\mathcal{P}} &= 0^{-}, 1^{+}, 2^{-}, 3^{+}, \dots & \text{ excluded by non-zero } \sin^{2}\theta_{1} \sin^{2}\theta_{2} \\ \diamond \text{ even normality:} \quad \mathcal{J}^{\mathcal{P}} &= 1^{-}, 3^{-}, \dots & \text{ excluded by non-zero } \sin^{2}\theta_{1} \sin^{2}\theta_{2} \\ \diamond \text{ rule out} & \mathcal{J}^{\mathcal{P}} &= 2^{+}, 4^{+} \text{ with:} \\ & \frac{d\sigma}{d\cos\theta} [gg/\gamma\gamma \to H \to ZZ] & \text{ only isotropic for spin 0} \end{aligned}$

• <u>Caveat</u>: HO corrections to $H \rightarrow WW/ZZ \rightarrow 4f$ distort the shapes of the distributions Bredenstein, Denner, Dittmaier, Walser

$\mathcal{D}etermination of \mathcal{S}pin and \mathcal{P}arity of \mathcal{SM} \mathcal{H}iggs, \mathcal{N}ecessary \mathcal{C}onditions$

• Standard Model:

 $\mathcal{T}_{00} = (M_H^2 - M_*^2 - M_Z^2) / (2M_*M_Z), \qquad \mathcal{T}_{11} = +\mathcal{T}_{-1,-1} = -1, \qquad \mathcal{T}_{10} = \mathcal{T}_{01} = \mathcal{T}_{1,-1} = 0$

Necessary conditions:

♦ Double polar angular distribution

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\cos\theta_1 d\cos\theta_2} = \frac{9}{16} \frac{1}{\gamma^4 + 2} \left[\gamma^4 \sin^2\theta_1 \sin^2\theta_2 + \frac{1}{2} \left(1 + \cos^2\theta_1 \right) (1 + \cos^2\theta_2) \right]$$

♦ Azimuthal angular distribution

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\phi} = \frac{1}{2\pi} \left[1 + \frac{1}{2} \frac{1}{\gamma^4 + 2} \cos 2\phi \right]$$

$$\gamma^2 = (M_H^2 - M_*^2 - M_Z^2) / (2M_*M_Z)$$

$\mathcal{D}etermination of \mathcal{S}pin and \mathcal{P}arity of \mathcal{SM} \mathcal{H}iggs, \mathcal{S}ufficient \mathcal{C}onditions$

•
$$\underline{M_H < 2M_Z}$$
: $d\Gamma/dM_*^2 \sim \beta$ for $\mathcal{J}^\mathcal{P} = 0^+$

 \Rightarrow only 0⁺ left (sufficient conditions)

• <u>Caveat</u>: HO corrections to $H \rightarrow WW/ZZ \rightarrow 4f$ distort the shapes of the distributions

Bredenstein, Denner, Dittmaier, Walser

\mathcal{P} seudoscalar A with $J^P = 0^-$

• Differential Distributions: Parity invariance ~>>

$$\frac{1}{\Gamma_A} \frac{d\Gamma_A}{d\cos\theta_1\cos\theta_2} = \frac{9}{64} (1 + \cos^2\theta_1)(1 + \cos^2\theta_2)$$
$$\frac{1}{\Gamma_A} \frac{d\Gamma_A}{d\phi} = \frac{1}{2\pi} \left[1 - \frac{1}{4}\cos 2\phi \right]$$

• Threshold Behaviour: $d\Gamma_A/dM_*^2 \sim \beta^3$

- If too small branching ratio $A \rightarrow Z^*Z$: sufficient and necessary conditions of spin/parity
 - Spin 0: isotropic angular distribution in $gg \to A \to \gamma \gamma$
 - Jets in $gg \rightarrow A + gg$ anti-correlated for pseudoscalar (correlated for scalar) Hagiwara eal
 - Exploit fermionic decay channels

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Azimuthal Angular Distributions: Parity

Choi, Miller, MMM, Zerwas

 $0^+: d\Gamma/d\varphi \sim 1 + f_{\rm kin}\cos 2\phi$, $0^-: d\Gamma/d\varphi \sim 1 - 1/4\cos 2\phi$

Threshold Behaviour: Spin

Choi, Miller, MMM, Zerwas

ATLAS *R*esults

ATI AS Phys.Lett.**B726**(2013)120

0⁻ rejected at 97.8% CL $(H \rightarrow ZZ^* \rightarrow 4l)$; 1[±] at \gtrsim 99.7% CL $(ZZ^* \rightarrow 4l, WW^* \rightarrow l\nu l\nu)$ 2⁺ rejected at \gtrsim 99.9% CL $(H \rightarrow \gamma\gamma, H \rightarrow ZZ^* \rightarrow 4l, H \rightarrow WW^* \rightarrow l\nu l\nu)$, indep $gg, q\bar{q}$

• $0^+, 0^-, 1^+, 1^-, 2^+, 2^-$ hypotheses in $H \to ZZ^* \to 4l$ PRL 110 (2013)

CMS-PAS-HIG-13-002

CMS-PAS-HIG-13-005

• Spin studies in $H \to WW^* \to l \nu l \nu$ CMS-PAS-HIG-13-003

(II) \mathcal{H} iggs- \mathcal{S} pin \mathcal{A} nalysis through $gg \to H^J \to \gamma\gamma \mathcal{D}$ ecays

- Systematic helicity analyses for angular distributions \rightsquigarrow
- Selection rules

from polar angular distribution spin-0: isotropic

Choi, Miller, MMM, Zerwas

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$\mathcal{D}istinction \ \mathcal{S}calar-type, \ \mathcal{T}ensor-type$

$\mathcal Discovered\ \mathcal Particle$ is the $\mathcal Higgs\ \mathcal Boson$

New results indicate that particle discovered at CERN is a Higgs boson

14 Mar 2013

Geneva, 14 March 2013. At the Moriond Conference today, the ATLAS and CMS collaborations at CERN¹'s Large Hadron Collider (LHC) presented preliminary new results that further elucidate the particle discovered last year. Having analysed two and a half times more data than was available for the discovery announcement in July, they find that the new particle is looking more and more like a Higgs boson, the particle linked to the mechanism that gives mass to elementary particles. It remains an open question, however, whether this is the Higgs boson of the Standard Model of particle physics, or possibly the lightest of several bosons predicted in some theories that go beyond the Standard Model. Finding the answer to this question will take time.

$\mathcal{E} x perimental \ \mathcal{V} erification \ of \ the \ EWSB \ \mathcal{M} echanism$

EWSB mechanism:

Creation of particle masses without violating gauge principles

The EWSB potential:

$$V(H) = \frac{1}{2!}\lambda_{HH}H^2 + \frac{1}{3!}\lambda_{HHH}H^3 + \frac{1}{4!}\lambda_{HHHH}H^4$$

${\mathcal T}$ rilinear coupling	$\lambda_{HHH} = 3 \frac{M_H^2}{v}$	
$\mathcal Q$ uartic coupling	$\lambda_{HHHH} = 3 \frac{M_H^2}{v^2}$	· · · · · · · · · · · · · · · · · · ·

${\cal M}$ easurement of the scalar boson self-couplings $ ightarrow$	\mathcal{E} xperimental verification
and	\mathcal{O} f the scalar sector of the
${\cal R}$ econstruction of the EWSB potential	${\cal E}{\sf WSB}$ mechanism

Determination of the scalar boson self-couplings at colliders:

λ_{HHH}	via pair production	ra
λ_{HHHH}	via triple production	T a

radiation off W/Z, WW/ZZ fusion, gg fusion
$\mathcal{T}he \ \mathcal{T}rilinear \ \mathcal{S}elf\text{-}\mathcal{C}oupling \ at \ the \ \mathcal{LHC}$

Determination of λ_{HHH} at the LHC

Djouadi, Kilian, MMM, Zerwas

double radiation of W/Z :	q ar q	\rightarrow	W/Z + HH	Barger,Han,Phillips;Baglio eal
WW/ZZ fusion:	qq	\rightarrow	qq + HH	Dicus,Kallianpur,Willenbrock Abbasabadi,Repko,Dicus,Vega Dobrovolskaya,Novikov Eboli,Marques,Novaes,Natale Liu-Sheng eal:Baglio eal
gluon gluon fusion:	gg	\rightarrow	HH	Glover,van der Bij Plehn,Spira,Zerwas Dawson,Dittmaier,Spira de Florian,Mazzitelli Grigo,Hoff,Melnikov,Steinhauser

gluon gluon fusion - dominant process



$\mathcal{D}ouble \ \mathcal{SM} \ \mathcal{S}calar \ \mathcal{B}oson \ \mathcal{P}roduction \ at \ the \ \mathcal{LHC}$



Djouadi, Kilian, MMM, Zerwas

$\mathcal{H}igher \ \mathcal{O}rder \ \mathcal{C}orrections \ to \ \mathcal{D}ouble \ \mathcal{H}iggs \ \mathcal{P}roduction$

Higher order corrections:

- \triangleright 2-loop QCD corrections $(M_H^2 \ll 4m_t^2) \sim 90 100\%$
- ▷ 2-loop QCD corrections $\sigma = \sigma_0 + \frac{\sigma_1}{m_t^2} + ... + \frac{\sigma_4}{m_t^8}$
- \triangleright NNLO soft+virtual QCD corrections: $\sim 20\% (M_H^2 \ll 4m_t^2)$
- \triangleright soft gluon resummation (SCET): ~ 30% ($M_H^2 \ll 4m_t^2$)

Dawson, Dittmaier, Spira

Grigo, Hoff, Melnikov, Steinhauser

de Florian, Mazzitelli

Shao, Li, Li, Wang



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$\mathcal{D}ouble \ \mathcal{H}iggs \ \mathcal{P}roduction \ \mathcal{P}rocesses$

Baglio, Djouadi, Gröber, MMM, Quevillon, Spira



Uncertainty (scale, pdf+ α_s , EFT) ggF at 14 TeV: ~ -30%... + 37%; VBF: ~ -7.5%... + 5%[For NLO cxns w/ parton shower, see also Frederix eal]

${\cal S}$ ensitivity to λ_{HHH}

Baglio, Djouadi, Gröber, MMM, Quevillon, Spira



 $gg \rightarrow HH : \Delta \sigma / \sigma \sim -\Delta \lambda / \lambda$ (decreasing with \sqrt{s}) Measurement of cross section with 50% accuracy yields 50% accuracy in λ_{HHH}

• Vast literature:

Baur,Plehn,Rainwater; Lafaye,Miller,Moretti,MMM; Osland,Pandita; M.Moretti eal; Arhrib eal; Asakawa eal; Dolan,Englert,Spannowski; Papaefstathiou,Yang,Zurita; Goertz,Papaefstathiou,Yang,Zurita; W. Yao; Contino eal; Gupta eal; No,Ramsey-Musolf; Barger,Everett,Jackson,Shaughnessy; deLima,Papaefstathiou,Spannowsky; ...

\mathcal{E} xpected \mathcal{A} ccuracies in λ_{HHH} at the \mathcal{LHC}

Small signal + large QCD background \rightsquigarrow challenge! Sample studies: $\underbrace{M_H < 140 \text{ GeV}: gg \rightarrow HH \rightarrow b\bar{b}\gamma\gamma:}_{0 \text{ SLHC }} Baur, Plehn, Rainwater$ $O \text{ SLHC } [\int \mathcal{L} = 6 \text{ ab}^{-1}]: M_H = 120 \text{ GeV} \quad \lambda_{HHH} = 0 \text{ exclusion} \text{ at } 90\% \text{ CL}$ $\underbrace{M_H = 125 \text{ GeV}: b\bar{b}\gamma\gamma, b\bar{b}\tau^+\tau^-, b\bar{b}W^+W^-:}_{0 \text{ b}\bar{b}\gamma\gamma, b\bar{b}\tau^+\tau^-, b\bar{b}W^+W^-:} Baglio, Djouadi, Gröber, MMM, Quevillon, Spira '12$ $o b\bar{b}\gamma\gamma, b\bar{b}\tau^+\tau^- look promising: <math>S/\sqrt{B} \approx 6 \text{ for } \int \mathcal{L} = 3 \text{ ab}^{-1}$

 $M_H = 125$ GeV: exploit subjet techniques:

Dolan, Englert, Spannowski'12 Papaefstathiou, Yang, Zurita'12

◦ LHC@14TeV [∫ L = 1000 fb⁻¹]: HHj → bb̄τ⁺τ⁻j: most promising to constrain λ_{HHH}
 ◦ LHC@14TeV [∫ L = 600 fb⁻¹]: HH → bb̄W⁺W⁻ → bb̄lνjj: strong evidence

 $M_H = 125$ GeV: exploit ratios of cross sections

Goertz, Papaefstathiou, Yang, Zurita '13

 $M_H = 125\,\,{
m GeV}:\, gg o HH o bar b \gamma\gamma$: (to be analysed experimentally)

Barger, Everett Jackson, Shaughnessy '13

• LHC@14 TeV $\left[\int \mathcal{L} = 3 \text{ ab}^{-1}\right]$: $\delta \lambda_{HHH} / \lambda_{HHH} = 40\%$ (?) \leftarrow multivariate analysis

\mathcal{E} xpected \mathcal{A} ccuracies in λ_{HHH} at the \mathcal{LHC}



◦ LHC@14 TeV [$\int \mathcal{L} = 3 \text{ ab}^{-1}$]: $\delta \lambda_{HHH} / \lambda_{HHH} = 40\%$ (?) ← multivariate analysis

 ${\mathcal B}$ eyond ${\mathcal T}$ he ${\mathcal S}$ tandard ${\mathcal M}$ odel

What About Beyond Standard Model (BSM) Physics?

Standard Model: incomplete picture of the universe

- SM has 19 free parameters: What are the values of these parameters?
- Common origin of all three forces of the SM?
- How to incorporte gravity?
- Candidate for Dark Matter (DM)? ...



Why Beyond Standard Model (\mathcal{BSM}) Physics?

Standard Model: incomplete picture of the universe

- SM has 19 free parameters: What are the values of these parameters?
- Common origin of all three forces of the SM?
- How to incorporte gravity?
- Candidate for Dark Matter (DM)? . . .



 $15^{10}\log Q$



Unification of the Coupling Constants in the SM and the minimal MSSM

10

0 i

 $1/\alpha_3$

5

10

 $15 \\ 10 \log Q$

10

0

0

 $1/\alpha_3$

10

5

Why Beyond Standard Model (BSM) Physics?

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Why Beyond Standard Model (BSM) Physics?

Standard Model: incomplete picture of the universe

- SM has 19 free parameters: What are the values of these parameters?
- Common origin of all three forces of the SM?
- How to incorporte gravity?
- Candidate for Dark Matter (DM)?

Supersymmetry: relates fermions and bosons

- \diamondsuit solves hierarchy problem
- \diamond gauge coupling unification (MSSM)
- ♦ Higgs mechanism generated radiatively
- \diamondsuit Cold Dark Matter candidate (\leftarrow R-parity) ...





Consequences: new particles (*e.g.* running in the loops), extended Higgs sectors (scalar, pseudoscalar Higgs bosons, Higgs bosons with no definite CP quantum number)



\mathcal{SUSY} Interpretation of the \mathcal{LHC} Higgs Results

Ø

...





$\mathcal M\textsc{any}$ good reasons for $\mathcal S\textsc{upersymmetry}$

- B Solution of the hierarchy problem
- $\ensuremath{\mathcal{B}}$ Gauge coupling unification
- Dark Matter candidate
- Dynamical generation of Higgs potential

- \square Maximal possible symmetry of the S-matrix
- $\ensuremath{\mathcal{B}}$ Way to incorporate gravity?

$\mathcal{T}he \ \mathcal{MSSM} \ \mathcal{H}iggs \ \mathcal{S}ector$





Higgs masses

M_h	\lesssim	$140~{\rm GeV}$	
$M_{A,H,H^{\pm}}$	\sim	$\mathcal{O}(v)1$ TeV	

Ellis et al;Okada et al;Haber,Hempfling; Hoang et al;Carena et al;Heinemeyer et al; Zhang et al;Brignole et al;Harlander et al Degrassi et al;Kant et al;...

Decoupling limit:

 $M_A \sim M_H \sim M_{H^\pm} \gtrsim v$ $M_h \to$ max. value, $\tan\beta$ fixed; h becomes SM-like

Modified couplings with respect to the SM: (decoupling limit Gunion, Haber)

Φ	$g_{\Phi u ar u}$	$g_{\phi d ar d}$	$g_{\Phi VV}$
h	$c_{\alpha}/s_{\beta} \rightarrow 1$	$-s_{\alpha}/c_{\beta} \rightarrow 1$	$s_{\beta-lpha} \rightarrow 1$
H	$s_{lpha}/s_{eta} ightarrow 1/\mathrm{tg}eta$	$c_{lpha}/c_{eta} ightarrow { m tg}eta$	$c_{eta-lpha} ightarrow 0$
A	$1/{ m tg}eta$	${ m tg}eta$	0



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$\mathcal{MSSM} \ \mathcal{H}iggs \ \mathcal{P}roduction \ at \ the \ \mathcal{LHC}$

Higgs boson production in the MSSM

• Gluon Fusion

 $pp \to gg \to h, H, A$

Additional squark loops



• W/Z Fusion

$$pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + h, H$$



• Higgs-strahlung

 $pp \to W^*/Z^* \to W/Z + h, H$



• Associated Production

 $pp \rightarrow t\bar{t}/b\bar{b} + h, H, A$





\mathcal{MSSM} $\mathcal{H}iggs$ $\mathcal{M}ass$ in $\mathcal{V}iew$ of the \mathcal{LHC} $\mathcal{R}esults$

• Vast literature on MSSM Higgs of $\sim 125~{ m GeV}$

Arbey eal; Li eal; Feng eal; Baer eal; Akula eal; Hall eal; Albornoz Vasquez eal; Heinemeyer eal; Desai et al.; Draper eal; Carena eal; Cao eal; Christensen eal; Kadastik eal; Buchmuller eal; Arvanitaki eal; Ellis eal; Curtin eal; Brummer eal; Barger eal; Hagiwara eal; Arbey eal; Blum eal; Beskidt eal; Baer eal; Giudice eal; Carena eal; Benbrik eal; Akula eal; Cahill-Rowley eal; Hirsch eal; ...

• Compatibility of MSSM Higgs mass with LHC Search

 \star Upper mass bound on SM-like Higgs with higher-order correction Δm_h

 $m_h^2 \approx M_Z^2 \cos^2 2\beta + \Delta m_h^2$

 $\star \Rightarrow M_H \approx 125 \text{ GeV}$ requires

 $\Delta m_h \approx 85 \text{ GeV} (\tan \beta \text{ large}) \Rightarrow \text{large corrections} \rightsquigarrow \text{'fine'-tuning}$

\mathcal{MSSM} $\mathcal{H}iggs$ $\mathcal{M}ass$ in $\mathcal{V}iew$ of the \mathcal{LHC} $\mathcal{R}esults$

Hall, Pinner, Ruderman 1112.2703



• Maximal stop mixing: $m_{\tilde{t}_1} \gtrsim 500 \text{ GeV}$

The \mathcal{NMSSM} Higgs Sector

Kim.Nilles

• Next-to-Minimal Supersymmetric Extension of the SM: NMSSM

Fayet; Kaul eal; Barbieri eal; Dine eal; Nilles eal; Frere eal; Derendinger eal; Ellis eal; Drees; Ellwanger eal; Savoy; Elliott eal; Gunion eal; Franke eal; Maniatis; Djouadi eal; Mahmoudi eal; ...

• The μ -problem of the MSSM:

Higgsino mass parameter μ must be of order of EWSB scale

• Solution in the NMSSM:

 μ generated dynamically through the VEV of scalar component of an additional chiral superfield field \hat{S} : $\mu = \lambda \langle S \rangle$

• Enlarged Higgs and neutralino sector:

7 Higgs bosons: $H_1, H_2, H_3, A_1, A_2, H^+, H^-$ 5 neutralinos: $\tilde{\chi}_i^0$ (i = 1, ..., 5)

• Significant changes of Higgs boson phenomenology

\mathcal{NMSSM} Higgs $\mathcal{M}ass$ in $\mathcal{V}iew$ of the \mathcal{LHC} Results

• Vast literature on NMSSM Higgs of $\sim 125~{ m GeV}$

Hall eal; Ellwanger; Gunion eal; King,MMM,Nevzorov; Albornoz Vasquez eal; Cao eal; Gabrielli eal; Ellwanger, Hugonie; Kang eal; Cheung eal; Jeong eal; Hardy eal; Kim eal; Arvanitaki eal; ...

• Compatibility of NMSSM Higgs mass with LHC Searches:

 \star Upper mass bounds + corrections to the MSSM, NMSSM Higgs boson mass:

MSSM: $m_h^2 \approx M_Z^2 \cos^2 2\beta + \Delta m_h^2$

NMSSM:
$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \Delta m_h^2$$

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\Rightarrow M_H \approx 125 requires:
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MSSM: $\Delta m_h \approx 85 \text{ GeV} (\tan \beta \text{ large}) \Rightarrow \text{ large corrections are needed } \rightarrow \text{ conflict with fine-tuning}$ NMSSM: $\Delta m_h \approx 55 \text{ GeV} (\lambda = 0.7, \tan \beta = 2)$

⇒ NMSSM requires less fine-tuning Hall,Pinner,Ruderman; Ellwanger; Arvanitaki,Villadoro; King,MMM,Nevzorov; Kang,Li,Li; Cao,Heng,Yang,Zhang,Zhu

\mathcal{NMSSM} Higgs $\mathcal{M}ass$ in $\mathcal{V}iew$ of the \mathcal{LHC} Results

Hall, Pinner, Ruderman 1112.2703



- $\diamond m_h$ maximized for small values of aneta
- $\circ m_h \approx 125 \text{ GeV}$ can be achieved also for zero mixing $X_t = 0$ and $m_{\tilde{t}_1} \ge 500 \text{ GeV}$

Thank you for your attention!

$\mathcal{H}iggs \ \mathcal{B}oson \ \mathcal{M}ass$

Higgs Boson Mass SM - fundamental parameter, not given by theory

- * self-consistency test of SM at quantum level (Higgs loop corrections to W boson mass)
- $\ast\,$ Higgs mass uncertainty feeds back in uncertainty on SM Higgs couplings
- $* M_H \leftrightarrow \text{stability of the electroweak vacuum}$
- * Test parameter relations in BSM theories (Higgs mass calculable; requires precise m_t)

Present Value from $H \rightarrow \gamma \gamma$ and $H \rightarrow ZZ^* \rightarrow 4l$ $M_H = 125.7 \pm 0.3 (\text{stat}) \pm 0.3 (\text{syst}) \text{ GeV}$ CMS-PAS-HIG-13-005

 $\rightarrow T$

Expected Precision

- * future measurements dominated by systematics
- $\ast\,$ interference effects signal and background, $\ldots\,$

Projected: $\delta M_H \sim 100/50$ MeV at LHC/HL-LHC

\mathcal{S} tability of the \mathcal{V} acuum



Degrassi et al. '12

Vacuum stability:

$$M_H > 129.4 \text{ GeV} + 1.4 \text{ GeV} \left(\frac{m_t - 173.2 \text{ GeV}}{0.7 \text{ GeV}}\right) - 0.35 \text{ GeV} \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007}\right) \pm 1.0_{\text{th}} \text{ GeV}$$

\mathcal{T} otal \mathcal{W} idth

Higgs Total Width $\Gamma_{H}\approx 4.4~{\rm MeV}$

• interference between Higgs signal $gg \to H \to \gamma\gamma$ and continuum $gg \to \gamma\gamma \rightsquigarrow$ Higgs mass shift

S.P.Martin '12,'13; Dixon,Li '13

• Off-shell $H \to Z^*Z^*$ production



Caola,Melnikov '13; Campbell,Ellis,Williams '13; Kauer,Passarino '12



Present Value - combined 4l and $2l2\nu$ final states

CMS Moriond '13 New!

 $\Gamma < 17$ MeV (35 MeV expected) $\,$ 95% CL $\,$

Projection to HL-LHC

dominated by systematics

e.g. $pp \rightarrow ZZ$ at NNLO QCD required, realistic target, see e.g.

Gehrmann, Tancredi, Weihs '13

\mathcal{I} nterferometry

